length represents a $\pi$ bond order of $c a 0 \cdot 25$, so the $\mathrm{S}-\mathrm{C}(5)$ bond length of $1.75 \AA$ should also represent a $\pi$ bond order of 0.25 (Cruickshank, 1961a,b). The double-bond length between $\mathbf{S}$ and C in thiourea (International Tables for X-ray Crystallography, 1962) is $1.710 \AA$, and the single-bond length for these two atoms is $1.83 \AA$ in aliphatic thiols (International Tables for X-ray Crystallography, 1962).

From the above evidence a double-bond character can be associated with the sulphamidic group and accordingly explained in terms of $\pi$-bonding molecular orbitals formed by $\mathrm{C}, \mathrm{N}$ and O atoms with the $3 d$ orbitals of $S$.

The packing of the molecules is illustrated in Fig. 2. There are no short intermolecular distances. Leastsquares planes are in Table 4.

We wish to thank Dr Moreno-Mañas for supplying the crystals used in this structural analysis and also for suggesting this work. The cooperation of the Centro de Proceso de Datos del Ministerio de Educación y Ciencia is acknowledged.

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# The Crystal and Molecular Structure of the Methanesulphonamide of $\boldsymbol{N}$-Methylpiperazine (Sulfan): $\mathbf{C}_{6} \mathbf{H}_{14} \mathbf{N}_{\mathbf{2}} \mathbf{S O}_{\mathbf{2}}$ 

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Crystals of the methanesulphonamide of $N$-methylpiperazine are monoclinic, space group $P 2_{1} / a$ with cell dimensions $a=15.405, b=8.488, c=6.940 \AA$ and $\beta=98.75^{\circ}$. Each unit cell contains four molecules. The structural model refined to $R=0.064$ for 1784 observed reflexions measured on an automatic four-circle diffractometer. The results are compared with those obtained previously on the methanesulphonamide of morpholine (MSM).

## Introduction

The study of the methanesulphonamide of $N$-methylpiperazine forms part of a wider structural study on the conformational analysis of saturated heterocycles (Katritzky \& Moreno-Mañas, 1974). The conformation of the N group in the ring of piperidine (Smith-Verdier, García-Blanco \& Florencio, 1976), morpholine (Perales \& Garcia-Blanco, 1977) and piperazine has been recently investigated.

## Experimental

Sulfan is a crystalline colourless solid: the material as supplied by Dr Moreno-Mañas yielded suitable crystals for study. Preliminary Weissenberg and precession photographs indicated monoclinic symmetry. Systematic absences for reflexions $h 0 l$ with $h \neq 2 n$ and $0 k 0$ with $k \neq 2 n$ specify space group $P 2_{1} / a$. Accurate cell parameters were obtained by a least-squares procedure applied to the setting angles of 36 reflexions

Table 1. Crystal data
Molecular formula $\mathrm{C}_{6} \mathrm{H}_{14} \mathrm{~N}_{2} \mathrm{O}_{2} \mathrm{~S}$
Molecular weight 178.134
Space group $P 2_{1} / a$
Monoclinic
$a=15.405$ (2) $\AA$
$b=8.488$ (2)
$c=6.940(1)$
$\beta=98.75(1)^{\circ}$

$$
\begin{aligned}
& V=896.8(2) \AA^{3} \\
& F(000)=384 \\
& \text { Radiation: } \lambda\left(\mathrm{Mo}^{-K} \alpha\right)=0.71069 \AA \\
& D_{c}=1.27 \mathrm{~g} \mathrm{~cm}^{-3} \\
& \mu=3.136 \mathrm{~cm}^{-1}
\end{aligned}
$$

measured on a Philips four-circle diffractometer and are given in Table 1 with other crystal data. 2580 reflexions were collected on a Philips PW 1100 diffractometer operating in the $\omega / 2 \theta$ scan mode with graphite-monochromated Mo Ka radiation. 1784 reflexions were taken as significantly above background as they were greater than $2 \sigma(I)$. Corrections were made for Lorentz and polarization factors but not for absorption. From a Wilson plot an overall temperature factor and scale factor were calculated, and these were used to normalize the structure factors (Karle \& Hauptman, 1956). The values for the statistical averages for the normalized structure factors correspond to a centrosymmetric structure.

## Determination and refinement of the structure

The position of the S atom was deduced from a sharpened three-dimensional Patterson function. A Fourier synthesis based on the signs determined by the S only gave maxima which could easily be interpreted as the eight non-hydrogen atoms of the sulfan molecule. The $R$ value at this stage, computed over 1200 terms, was $0 \cdot 25$. The refinement was carried out by a full-matrix least-squares method. Only observed experimental data were used in the refinement. Four cycles of isotropic refinement followed by three cycles of anisotropic least-squares refinement reduced the $R$ value to $0 \cdot 10$. At this stage a three-dimensional difference synthesis was computed and peaks at or near the expected H positions were chosen. The H atoms were included in the refinement with isotropic thermal parameters. The weighting scheme was: $w=K w_{1} w_{2}$ with $w_{1}=1 / \sigma_{f}^{2}$ and $w_{2}=1 / \sigma_{s}^{2}$, and $\sigma_{f}$ and $\sigma_{s}$ as follows:

$$
\begin{array}{lll}
\sigma_{f}=\left(0.7589+0.0644\left|F_{0}\right|\right) & \text { if } \quad 0<\left|F_{0}\right|<2.44, \\
\sigma_{f}=\left(1.1948-0.1216\left|F_{0}\right|\right) & \text { if } \quad 2.44<\left|F_{0}\right|<6.30, \\
\sigma_{f}=\left(0.3982+0.0158\left|F_{0}\right|\right) & \text { if } \quad 6.30<\left|F_{0}\right|<15.83, \\
\sigma_{f}=\left(-0.2735+0.0480\left|F_{0}\right|\right) & \text { if } 15.83<\left|F_{0}\right|<125.86, \\
\sqrt{ } \sigma_{s}=(2.3125-4.0609 s) & \text { if } & 0<\left|F_{0}\right|<0.390, \\
\sqrt{ } \sigma_{s}=(-0.3723+2.8931 s) & \text { if } & 0.390<\left|F_{0}\right|<0.4550, \\
\sqrt{ } \sigma_{s}=(1.8483-1.9380 s) & \text { if } & 0.4550<\left|F_{0}\right|<0.5500, \\
\sqrt{ } \sigma_{s}=(-1.1953+3.5980 s) & \text { if } & 0.5500<\left|F_{0}\right|<0.6600, \\
\sqrt{ } \sigma_{s}=(5.0468-5.7543 s) & \text { if } & 0.6600<\left|F_{0}\right|<0.7000,
\end{array}
$$

where $s$ is $\sin \theta / \lambda$ and $K=1.0017$.

Table 2. Positional parameters $\left(\times 10^{4}\right)$ for non-hydrogen atoms

|  | $x$ | $y$ | $z$ |
| :--- | ---: | :---: | ---: |
|  | $x$ | $y$ | $z$ |
| S | $2268(0)$ | $3109(1)$ | $6684(1)$ |
| $\mathrm{O}(1)$ | $3056(1)$ | $3080(4)$ | $5838(4)$ |
| $\mathrm{O}(2)$ | $2161(2)$ | $1977(3)$ | $8158(3)$ |
| $\mathrm{N}(1)$ | $1452(1)$ | $2851(3)$ | $4917(3)$ |
| $\mathrm{N}(2)$ | $-78(2)$ | $2952(3)$ | $2060(3)$ |
| $\mathrm{C}(1)$ | $577(2)$ | $2602(4)$ | $5474(4)$ |
| $\mathrm{C}(2)$ | $-16(2)$ | $1904(4)$ | $3740(5)$ |
| $\mathrm{C}(3)$ | $794(2)$ | $3185(4)$ | $1525(4)$ |
| $\mathrm{C}(4)$ | $1414(2)$ | $3896(4)$ | $3198(4)$ |
| $\mathrm{C}(5)$ | $2144(2)$ | $5009(4)$ | $7632(5)$ |
| $\mathrm{C}(6)$ | $-670(3)$ | $2295(5)$ | $413(6)$ |

Table 3. Hydrogen fractional coordinates $\left(\times 10^{3}\right)$, thermal parameters ( $\times 10^{2}$ ) and $\mathrm{C}-\mathrm{H}$ bonds $(\AA)$

|  | $x$ | $y$ | $z$ | $U$ | $\mathrm{C}-\mathrm{H}$ |
| :--- | ---: | :---: | :---: | :---: | :---: |
|  | $x$ | $y$ |  |  |  |
| $\mathrm{H}(1)$ | $33(3)$ | $362(5)$ | $579(6)$ | $3.4(1 \cdot 1)$ | $0.98(4)$ |
| $\mathrm{H}(2)$ | $69(2)$ | $187(4)$ | $659(6)$ | $4.5(1.0)$ | $0.99(4)$ |
| $\mathrm{H}(3)$ | $-58(2)$ | $169(4)$ | $411(5)$ | $4.0(1.0)$ | $0.97(4)$ |
| $\mathrm{H}(4)$ | $21(2)$ | $86(4)$ | $334(5)$ | $4.4(0.9)$ | $1.00(4)$ |
| $\mathrm{H}(5)$ | $75(2)$ | $395(4)$ | $39(4)$ | $2.7(0.7)$ | $1.02(3)$ |
| $\mathrm{H}(6)$ | $105(2)$ | $223(4)$ | $113(5)$ | $3.7(0.8)$ | $0.96(3)$ |
| $\mathrm{H}(7)$ | $198(2)$ | $404(4)$ | $291(5)$ | $4.7(0.9)$ | $0.94(4)$ |
| $\mathrm{H}(8)$ | $122(2)$ | $497(4)$ | $357(5)$ | $2.6(0.8)$ | $1.01(3)$ |
| $\mathrm{H}(9)$ | $222(2)$ | $579(4)$ | $671(4)$ | $4.2(0.7)$ | $0.94(3)$ |
| $\mathrm{H}(10)$ | $254(2)$ | $509(4)$ | $865(4)$ | $3.5(0.7)$ | $0.86(3)$ |
| $\mathrm{H}(11)$ | $151(2)$ | $511(4)$ | $790(5)$ | $5.1(0.8)$ | $1.02(4)$ |
| $\mathrm{H}(12)$ | $-51(4)$ | $125(8)$ | $0(9)$ | $3.5(2.0)$ | $0.97(7)$ |
| $\mathrm{H}(13)$ | $-67(5)$ | $311(9)$ | $-71(10)$ | $6.1(2.4)$ | $1.04(7)$ |
| $\mathrm{H}(14)$ | $-123(5)$ | $218(8)$ | $90(9)$ | $5.8(2.1)$ | $0.98(7)$ |

Further cycles of anisotropic refinement of the heavy atoms with the H atoms treated isotropically gave final weighted and unweighted $R$ values of 0.060 and 0.064 respectively $\left[R_{w}=\left(\Sigma w \Delta^{2} / \Sigma w\left|F_{o}\right|^{2}\right)^{1 / 2}\right]$ with $\left\langle w \Delta^{2}\right\rangle$ showing no trends.

The atomic scattering factors for all atoms were taken from International Tables for X-ray Crystallography (1974).
The final atomic parameters for non-hydrogen atoms are given in Table 2, and those of the H atoms together with $\mathrm{C}-\mathrm{H}$ distances in Table 3.

All the calculations were performed with the XRAY 70 system of crystallographic programs and carried out on a Univac 1108 computer.*

## Results and discussion

The sulfan molecule, with the labelling of atoms, is shown in Fig. 1. The bond lengths and angles are

[^0]collected in Table 4. The piperazine ring has a chair conformation and a non-crystallographic plane of symmetry through the $N(1)-N(2)$ atoms which is normal to the $C(1)-C(2)-C(3)-C(4)$ chair plane. All


Fig. 1. A view of the sulfan molecule showing the atomic numbering.

Table 4. Interatomic distances and angles

| $\mathrm{S}-\mathrm{O}(1)$ | $1.426(2) \AA$ | $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(2)$ | $118.7(2)^{\circ}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{S}-\mathrm{O}(2)$ | $1.431(3)$ | $\mathrm{O}(2)-\mathrm{S}-\mathrm{N}(1)$ | $107.1(1)$ |
| $\mathrm{S}-\mathrm{N}(1)$ | $1.633(2)$ | $\mathrm{O}(1)-\mathrm{S}-\mathrm{C}(5)$ | $108.5(2)$ |
| $\mathrm{S}-\mathrm{C}(5)$ | $1.764(3)$ | $\mathrm{O}(2)-\mathrm{S}-\mathrm{N}(1)$ | $106.7(1)$ |
| $\mathrm{N}(1)-\mathrm{C}(1)$ | $1.47(4)$ | $\mathrm{O}(2)-\mathrm{S}-\mathrm{C}(5)$ | $108.5(2)$ |
| $\mathrm{N}(1)-\mathrm{C}(4)$ | $1.481(4)$ | $\mathrm{N}(1)-\mathrm{S}-\mathrm{C}(5)$ | $106.7(1)$ |
| $\mathrm{N}(2)-\mathrm{C}(2)$ | $1.458(4)$ | $\mathrm{S}-\mathrm{N}(1)-\mathrm{C}(1)$ | $116.9(2)$ |
| $\mathrm{N}(2)-\mathrm{C}(3)$ | $1.459(4)$ | $\mathrm{S}-\mathrm{N}(1)-\mathrm{C}(4)$ | $117.1(2)$ |
| $\mathrm{N}(2)-\mathrm{C}(6)$ | $1.462(4)$ | $\mathrm{C}(1)-\mathrm{N}(1)-\mathrm{C}(4)$ | $111.9(2)$ |
| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1.517(4)$ | $\mathrm{C}(2)-\mathrm{N}(2)-\mathrm{C}(3)$ | $109.7(2)$ |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $1.513(4)$ | $\mathrm{C}(2)-\mathrm{N}(2)-\mathrm{C}(6)$ | $110.5(3)$ |
|  |  | $\mathrm{C}(3)-\mathrm{N}(2)-\mathrm{C}(6)$ | $110.0(3)$ |
|  |  | $\mathrm{N}(1)-\mathrm{C}(1)-\mathrm{C}(2)$ | $108.3(3)$ |
|  |  | $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{N}(2)$ | $110.7(3)$ |
|  |  | $\mathrm{N}(2)-\mathrm{C}(3)-\mathrm{C}(4)$ | $110.9(2)$ |
|  |  | $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{N}(1)$ | $108.8(3)$ |

the bond angles in this piperazine ring, except that at $N(1)$, are close to $110^{\circ}$ including the angle at the $N(2)$ atom; the other outer angles at $N(2)$ are also near this value. The average $\mathrm{N}-\mathrm{C}$ distance for $\mathrm{N}(1)-\mathrm{C}$ is $1.484 \AA$. This distance is approximately equal to that found in the dihydrochloride of piperazine ( $1.49 \AA$ ) where Rérat (1960) observed i symmetry for the piperazinium ion. The average $N(2)-C$ distance is on the other hand $1.466 \AA$. This value is close to the $\mathrm{N}-\mathrm{C}$ bond length $1.458 \AA$ found in the hexahydrate of piperazine where Schwarzenbach (1968) found $2 / m$ symmetry for the piperazine ring. In these compounds all the bond angles in the hetero ring are near $110^{\circ}$. In the present work the ring has a noncrystallographic centre of symmetry. The obvious lack of a centre of symmetry could tentatively be explained as due to the difference between the two N atoms; $\mathrm{N}(2)$ is tetrahedral, whereas $N(1)$ is close to trigonal. Thus, the sums of the three angles around these atoms are $346^{\circ}$ for $\mathrm{N}(1)$ and $330^{\circ}$ for $\mathrm{N}(2)$. The displacements of the N atoms from the plane defined by the three surrounding atoms are $N(1)=-0.33 \AA$ and $N(2)=$ $0.47 \AA$ (Table 5).

These results suggest that $N(1)$ has a larger contribution from an $s p^{3}$-hybridized configuration than from an $s p^{2}$. This is indicated by the above mentioned displacement of the plane. Furthermore, the $\mathrm{S}-\mathrm{N}$ length decreases $(1.63 \AA)$ from the observed singlebond $(1.76 \AA)$ value because of the contribution from the nitrogen lone pair, which is consistent with the opening of the $\mathrm{S}-\mathrm{N}-\mathrm{C}$ angles ( $117^{\circ}$ ). In a previous work (Perales \& Garcia-Blanco, 1977) the MSM molecule was found to present an identical situation. Both compounds appear to be unaffected by the eventual $\pi$-electron delocalization from $S$ through $N$ to the ring system. However, the hybridization of the $N(1)$ atom is responsible for the relative orientation of the $\mathrm{C}-\mathrm{N}-\mathrm{S}$ and $\mathrm{O}-\mathrm{S}-\mathrm{O}$ planes. In both compounds the mean value for the angle between these two planes is $56^{\circ}$ which is similar to $58^{\circ}$ for the $s p^{3} \mathrm{~N}$ atoms and

Table 5. Least-squares planes

Plane I

|  | $\Delta$ |
| :--- | ---: |
|  |   <br> $\mathrm{C}(1)$ $-0.005 \AA$ <br> $\mathrm{C}(2)$ 0.005 <br> $\mathrm{C}(3)$ -0.005 <br> $\mathrm{C}(4)$ 0.005 <br> $\mathrm{~N}(1)^{*}$ 0.663 <br> $\mathrm{~N}(2)^{*}$ -0.679 <br> $\mathrm{~S}^{*}$ 1.157 l |

Plane II

|  | $\Delta$ |
| :--- | ---: |
|  | N |
| $\mathrm{N}(1)$ | $0.000 \AA$ |
| $\mathrm{C}(1)$ | 0.000 |
| $\mathrm{C}(4)$ | 0.000 |
| $\mathrm{~S}^{*}$ | 0.953 |
| $\mathrm{C}(2)^{*}$ | -1.222 |
| $\mathrm{C}(3)^{*}$ | -1.207 |

Plane III

|  | $\Delta$ |
| :--- | ---: |
| S | $0.000 \AA$ |
| $\mathrm{C}(1)$ | 0.000 |
| $\mathrm{C}(4)$ | 0.000 |
| $\mathrm{~N}(1)^{*}$ | -0.335 |

Plane IV

|  |  |
| :--- | :--- |
| $\mathrm{C}(2)$ | $0.000 \AA$ |
| $\mathrm{C}(3)$ | 0.000 |
| $\mathrm{C}(6)$ | 0.000 |
| $\mathrm{~N}(2)^{*}$ | 0.472 |

Dihedral angles between the planes $\left({ }^{\circ}\right)$

| Plane | II | III | IV |
| :---: | :---: | :---: | :---: |
| I | 53.34 | 29.44 | 19.72 |

* Atom not included in definition of the plane.


Fig. 2. The molecular packing viewed down $\mathbf{b}$.
contrasts with the $87^{\circ}$ value for the $s p^{2}$ (Cameron, Prout, Denton, Spagna \& White, 1975).
The conformation of the $\mathrm{SO}_{2}-\mathrm{CH}_{3}$ moiety with respect to the $\mathrm{N}(1)$ ring is equatorial. The deviations of the $\mathrm{N}(1)$ and S atoms from the chair plane $\mathrm{C}(1)-$ $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(4)$ are 0.66 and $1.16 \AA$ respectively. This deviation is $0.5 \AA$ larger for the $S$ atom than for $\mathrm{N}(1)$ and corresponds to an angle of $18^{\circ}$ with respect to the chair plane. An identical situation is found in the MSM molecule where the deviation is $0.38 \AA$ corresponding to an angle of $13^{\circ}$.

The packing of the molecules is shown in Fig. 2. Intermolecular distances shorter than the van der Waals radii are not observed.

We wish to thank Dr Moreno-Mañas for providing the sulfan crystals. We also thank the Centro de

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[^0]:    * Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 32652 ( 13 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 1NZ, England.

